RET FRC Model Solutions Fall 2021

1. Learning Objectives:

- 1. The candidate will understand how to analyze data for quality and appropriateness.
- 7. The candidate will understand how to apply the standards of practice and professional conduct guidelines.

Learning Outcomes:

(1a) Identify data needed.

- (1b) Assess data quality.
- (1c) Make and/or recommend appropriate assumptions where data cannot be provided.
- (1d) Comply with regulatory and professional standards pertaining to data quality.

Sources:

ASOP 23

Does your pension data need a refresh

CSOP 1440, 1510, 1530

Commentary on Question:

Candidates generally did well on part a, but less so on part b. Most candidates discussed the SOP related to disciplinary action, assuming the actuary of Company XYZ had made a mistake in their calculations rather than focusing on the SOP related to Data (CSOP1440), using another Actuary's work (CSOP 1510 and 1530)

Solution:

(a) Identify the data required for each group of membership to verify the liabilities.

The data queries should include the following information as at date of asset transfer for the different groups of members:

Actives members:

- Name/ID number
- Date of birth
- Gender
- Date of hire/date of membership or employment vs pensionable services
- Accrued pension amount at transfer date (monthly or annual)

Deferred vested members:

- Name/ID number
- Date of birth
- Gender
- Unreduced retirement date/age and unreduced pension amounts
- Accrued pension amount at normal retirement (monthly or annual)

Retirees and surviving spouse:

- Name/ID number
- Date of birth (retirees and surviving spouse)
- Gender
- Date of retirement
- Date of death for member
- Date of death for surviving spouse, (for joint and last survivor option) if applicable
- Pension forms (JS or LA, with guaranteed period, if applicable)
- Date of birth of spouse (if JS option) and gender
- Pension amount (monthly or annual)
- (b) Recommend a course of action, taking into consideration professional standards.
 - 1. The following actions relate to Data (CSOP 1440):
 - Perform data check regarding competence and integrity of the data; and assess whether the data are sufficient and realiable.
 - <u>F</u>or examples,
 - Perform reasonableness check on the data (e.g. are the date of birth/ date of retirement within a reasonable range? Are the pensionable service consistent with the date of membership? Pension payments are consistent with the pension register)
 - Ask for a copy of the latest valuation reports and compare the data/summary statistics.
 - Perform a sanity check of the data based on plan provisions (are the pension amounts consistent with pensionable services? Are the unreduced earliest retirement date/age consistent with the plan provisions?)
 - 2. The following actions relate to the review or repeat of another actuary's work [CSOP 1530]:
 - Materiality You should determine if the discrepancy is material. In this case, the lower liabilities calculated from the other actuary means a smaller asset amount will be transferred and 15% of discrepancy is material. Further investigation is required and notify the client.

- You may wish to request for individual liabilities and compare to yours and determine if the discreapncies may be due to an identiable group of member or due to data error of individual members.
- Review if the assumptions used by another actuary is appropriate and justifiable for the purpose of the work. The assumptions used are in fact the same as those disclosed.
- Based on your review of the work (if data issues not being resolved), engage the other actuary and consider whether the interests of the actuary's client or employer and the reviewer's client or employer are opposed.
- **3.** The following action relate to an actuary's consideration of using another person's work (CSOP 1510):
 - An actuary may consider using and taking responsibility for another person's work if such actions are justified. Given the materiality of the discrepancies in this case, you should not use nor take responsibility for another person's work.

3. The candidate will understand how to apply/synthesize the methods used to value pension benefits for various purposes.

Learning Outcomes:

- (3a) Differentiate between the various purposes for valuing pension plans:
 - (i) Funding
 - (ii) Solvency
 - (iii) Termination/wind-up/conversion
- (3b) Perform periodic valuations of ongoing plans, calculating normal cost and actuarial liability, using a variety of cost methods.
- (3c) Analyze and communicate the pattern of cost recognition that arises under a variety of funding methods
- (3d) Analyze and communicate the impact on cost stability of a variety of asset valuation methods.
- (3e) Perform valuations for special purposes, including:
 - (i) Plan termination/wind-up/conversion valuations
 - (ii) Hypothetical wind-up and solvency valuations
 - (iii) Open group valuations
 - (iv) Share risk pension plan valuations
- (3f) Calculate actuarially equivalent benefits.

Sources:

CIA Consolidated Standards of Practice, sections 3100-3500

Educational Note: Section 3500 of the Practice-Specific Standards for Pension Plans – Pension Commuted Values (Subsection 3570) - see attached

Educational Note: Section 3500 of the Practice-Specific Standards for Pension Plans – Pension Commuted Values (other than Subsection 3570) - see attached

Commentary on Question:

Commentary listed underneath question component.

Solution:

(i) Calculate the discount rates applicable to commuted value calculations for terminations in January 2022.

Commentary on Question:

Most candidates performed well on this question. Many candidates failed to receive full marks due to one or more of the following.

- Failing to annualize the semi-annual published rates
- Failing to recognize the one-month lag required by the standard
- Incorrectly calculating the spread on provincial and federal bonds in many cases a spread was not calculated, and the candidate used one of the provincial or federal bond rates in place of the spread
- Final rates were not rounded

Candidate is expected to show the following to get full points:

| i 7 (annualized) | 0.48058% |
|--|----------|
| i _L (annualized) | 1.24384% |
| Mid-Term Provincial Bond Index (annualized) | 1.10705% |
| Long-Term Provincial Bond Index (annualized) | 2.02010% |
| Mid-Term Corporate Bond Index (annualized) | 1.85149% |
| Long-Term Corporate Bond Index (annualized) | 2.89871% |
| Mid-Term Federal Non-Agency Bond Index (annualized) | 0.61494% |
| Long-Term Federal Non-Agency Bond Index (annualized) | 1.12716% |

• Annualize published figures (from December rates): (1+i/2)^2-1

- Calculate spread components:
 - PS 1-10 = (FTSE Canada Mid-term Provincial bond index yield, annualized FTSE Canada Mid-term Federal non-agency bond index yield, annualized) = 0.49210%
 - CS ₁₋₁₀ = (FTSE Canada Mid-term Corporate bond index yield, annualized FTSE Canada Mid-term Federal non-agency bond index yield, annualized) = 1.23655%
 - PS ₁₀₊ = (FTSE Canada Long-term Provincial bond index yield, annualized FTSE Canada Long-term Federal non-agency bond index yield, annualized) = 0.89294%
 - CS 10+ = (FTSE Canada Long-term Corporate bond index yield, annualized FTSE Canada Long-term Federal non-agency bond index yield, annualized) = 1.77155%
- Calculate spreads:
 - $S_{1-10} = 0,667 * PS_{1-10} + 0,333 * CS_{1-10} = 0.74000\%$

 $S_{10+} = 0,667 * PS_{10+} + 0,333 * CS_{10+} = 1.18552\%$

• Calculate the discount rates:

| i 1-10 | $= i_{7} + S_{1-10}$ | = 1.22058% (1.20% rounded) |
|------------------|---------------------------------------|----------------------------|
| i ₁₀₊ | = $i_L + 0,5 * (i_L - i_7) + S_{10+}$ | = 2.81100% (2.80% rounded) |

(ii) Calculate the commuted value for each active member assuming they voluntarily terminated employment on January 1, 2022.

Commentary on Question:

Most candidates performed well on this question, recognizing that members 1 and 2 are not eligible for grow-in (voluntary termination) or bridge benefits, and the result of the CV retirement assumption is age 65.

| Member | 1 | 2 |
|----------|--|--|
| FAE | = (\$85,000 + \$79,000 + \$75,000) / 3 | = (\$102,000 + \$100,000 + \$97,500) / 3 |
| | = \$79,666.67 | = \$99,833.33 |
| Benefit | = 1.25% x FAS x Years of service | = 1.25% x FAS x Years of service |
| | = 1.25% x 79,666,67 x 9 years | = 1.25% x 99,833,33 x 11 years |
| | = \$8,962.50 | = \$13,727.08 |
| Best Age | 65 | 65 |
| EURA | 65 | 65 |
| Factor | 8.7 | 11.3 |
| CV | = (8.7 x \$8,962.50 x 1.0) | = (11.3 x \$13,727.08 x 1.0) |
| | = \$77,973.75 | = \$155,116.04 |

(iii) Calculate the commuted value for each active member assuming the plan was wound up on January 1, 2022.

Commentary on Question:

Most candidates performed well on this question, recognizing that member 1 did not meet grow-in eligibility and member 2 did meet the 55 point grow-in eligibility requirement.

Determining grow-in eligibility: Age + service greater than 55 points

- Member 1: 35 + 9 = 44 (not eligible for grow-in)
- Member 2: 45 + 11 = 56 (eligible for grow-in)

Member 1 CV is same as Part A.

Member 2:

| Age | Factor (pension) | Factor (bridge) | Reduction (pension) | Commuted value |
|-----|------------------|-----------------|---------------------|----------------|
| 55 | 18.5 | 0 | 0.85 | 215,858.39 \$ |
| 56 | 17.6 | 0 | 0.88 | 212,605.07 \$ |
| 57 | 16.9 | 0 | 0.91 | 211,108.81 \$ |
| 58 | 16.1 | 0 | 0.94 | 207,745.68 \$ |
| 59 | 15.3 | 0 | 0.97 | 203,723.64 \$ |
| 60 | 14.6 | 0 | 1 | 200,415.42 \$ |
| 61 | 13.9 | 0 | 1 | 190,806.46 \$ |
| 62 | 13.3 | 2.1 | 1 | 201,050.21 \$ |
| 63 | 12.6 | 1.4 | 1 | 185,281.25 \$ |
| 64 | 12 | 0.7 | 1 | 170,885.00 \$ |
| 65 | 11.3 | 0 | 1 | 155,116.04 \$ |

Member 2 retirement assumption:

- 50% at age of highest commuted value (age 55) = \$215,858.39
- 50% at age of unreduced pension (age 60) = \$200,415.42

Member 2 CV = 0.5 x \$215,858.39 + 0.5 x \$200,415.42 = 208,136.90

 (iv) Describe how the calculation of the commuted value would differ if the plan were a target benefit plan in accordance with the Canadian Institute of Actuaries' Standards of Practice.

Commentary on Question:

Candidates did not perform as well in this section of the question. In particular, many candidates could only identify some points related to CV calculations differences under a target benefit plan.

- CVs are calculated using the same going concern assumptions as used in the latest actuarial valuation report or cost certificate filed with applicable pension legislator.
- Going concern assumptions used for the CV calculations would not include any margins or provisions for adverse deviations unless required by applicable legislation or terms of the plan.
- Discount rate would be net of any adjustment for investment expenses.
- Discount rate would be net of any adjustment for non-investment expenses expected to be paid from plan's assets if required by applicable legislation or terms of the plan.

- Mortality assumption appropriate for overall plan membership and would not vary for different subsets of plan population (other than age and gender).
- When calculating the CV of a deferred pension, assumptions used would be assumptions that are appropriate for purposes of performing actuarial valuation only for deferred pensioners of the plan (e.g., assumed retirement age of deferreds).
- May be adjusted to reflect funded status of the pension plan only as required by applicable legislation or by the terms of the plan.

- 3. The candidate will understand how to apply/synthesize the methods used to value pension benefits for various purposes.
- 6. The candidate will understand how to apply the regulatory framework in the context of plan funding.

Learning Outcomes:

(3b) Perform periodic valuations of ongoing plans, calculating normal cost and actuarial liability, using a variety of cost methods.

Sources:

Canadian Pensions and Retirement Income Planning, Willis Towers Watson, 6th Edition, 2017

• Ch. 15 (excluding Section 1525)

Morneau Shepell, Handbook of Canadian Pension and Benefit Plans, 17th Edition, 2020

• Ch. 3 and 6

Pension Mathematics for Actuaries, Anderson, Arthur W., 3rd Edition, 2006

• Ch. 1-4 and 7

FR-108-13: Pension Funding Exercises (background only)

Calculation of Incremental Cost on a Hypothetical Wind-Up or Solvency basis, CIA Educational Note, Dec 2010

Commentary on Question:

Candidates were asked to perform full going concern and wind-up valuations including gain and loss and determination of contributions. While candidates were able to successfully complete some portions of the question, candidates struggled with other portions. Minor calculation errors were tracked through and resulted in minimal deductions if the rest of the calculations were done correctly.

Solution:

(a) Calculate the total normal cost, going concern liability and the unfunded actuarial liability as at January 1, 2021.

Commentary on Question:

Overall this part of the question was done well by candidates. Many candidates struggled with determining the market value of assets as mistaken components were added in or excluded.

| Mark | et value | of assets | | 2,911,840 | | | | | |
|--|---|---|--|---|--|---|--|---|---|
| Going | conceri | n funding target | | | | | | | |
| Going | concern | liabilities: | | | | | | | |
| U | ve memb | | | 1,411,749 | | | | | |
| | | | <u> </u> | | | | | | |
| | erred pen | sioners | | 94,439 | | | | | |
| Pens | ioners | | | 1,235,257 | | | | | |
| Subtot | al | | | 2,741,444 | | | | | |
| PfAD | | | | 274,144 | | | | | |
| Total | | | | | | | | | |
| Total | | | | 3,015,589 | | | | | |
| Fundi | ng exces | s (shortfall) | | (103,749) | | | | | |
| | | | With | out PfAD | Wit | th PfAD | | | |
| Norm | al cost | | | 57,293 | | 63, |)22 | | |
| ACTU | AL ASSE | rs | | | | | | | |
| 1.1.202 | 20 Market | Value of Assets | | 2,5 | 500,000 | | | | |
| 2020 r | eturn on a | assets | | : | 300,000 | | | | |
| Employ | ver contril | outions remitted at 12.3 | 31.2020 | | 150,000 | | | | |
| Employ | | | | | | | | | |
| | | yments with Interest | | | -38,160 | | | | |
| 2020 E | Benefit Pa | | | | | | | | |
| 2020 E | Benefit Pa 21 Marke | yments with Interest | | 2,9 | -38,160 11,840 Retirement | | | | |
| 2020 E 1.1. 20 2 | Benefit Pa 21 Marke t | yments with Interest | | 2,9 Termination 6 0.295 | -38,160 11,840 Retirement 5 60 5 0.3736 | i | | | |
| 2020 E 1.1. 20 2 | Benefit Pa 21 Marke Member 1 Age V Actuarial Liability | yments with Interest | 3,; 249,; | 2,9 Termination 6 0.295 560 32' 366 16,515 | -38,160 11,840 Retirement 5 0.3736 3,239 | | | | |
| 2020 E 1.1.202 ACTIVES | Senefit Pa 21 Marke Member 1 Age V Actuarial Liability Normal Cost | yments with Interest t Value of Assets | 3,6 249,7 19,7 | 2,9 Termination 6 0.295 560 322 366 116,519 182 | -38,160 11,840 5 0.3736 3,239 2 232,848 | 38,871.82 | decrement | survival P | PUC |
| 2020 E 1.1.20 ACTIVES Proj. Date 1/1/2018 | Benefit Pa 21 Marke Age v Actuarial Liability Normal Cost Age | yments with Interest | 3, 249, 19, <u>Salary</u> 83,(| 2,9 Termination 6 0.2955 560 327 366 16,519 182 FAE 500 | -38,160 11,840 Retirement 5 0.3736 3,239 | i | decrement | survival P | PUC |
| 2020 E 1.1.20 ACTIVES Proj. Date 1/1/2018 1/1/2019 | Benefit Pa 21 Marker Age V Actuarial Liability Normal Cost Age | yments with Interest t Value of Assets | 3,5 249,3 19,1 Salary 83,(85,0 | 2,9 Termination 6 0.295 560 322 366 16,515 182 FAE 500 500 | -38,160 11,840 5 0.3736 3,239 2 232,848 | 38,871.82 | decrement | survival P | PUC |
| 2020 E 1.1.20 2 ACTIVES Proj. Date 1/1/2018 | Benefit Pa 21 Marker Age V Actuarial Liability Normal Cost Age | yments with Interest t Value of Assets | 3, 249, 19, <u>Salary</u> 83,(| 2,9 Termination 6 0.295 560 322 366 16,515 182 FAE 500 000 000 | -38,160 11,840 5 6 6 6 6 6 6 6 6 7 8 8 8 7 8 8 8 8 7 8 8 8 7 8 8 8 7 8 8 8 7 8 8 8 8 7 8 8 8 8 8 7 8 9 8 8 8 8 | 38,871.82 | decrement | survival P | PUC |
| 2020 E 1.1.202 AcTives Proj. Date 1/1/2018 1/1/2020 1/1/2021 1/1/2021 | Benefit Pa 21 Marke Member 1 Age V Actuarial Liability Normal Cost Age 39 40 | yments with Interest t Value of Assets | 3,5 249,3 19, Salary 83,0 85,0 98,0, 108,0 111,2 | Termination 6 0.295 0.295 386 16,519 FAE 000 000 000 000 88,667 240 97,000 | -38,160 11,840 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP | 38,871.82 Discount 1.0000 0.9542 | - 0.10 | 1.0000 | - 194 |
| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2022 1/1/2022 1/1/2022 | Benefit Pa 21 Marke Actuarial Liability Normal Cost Age 39 40 41 | yments with Interest t Value of Assets | 3,; 249,; 19,7 Salary 83,(85,(98,(108, 111,2 111,2 | Termination 6 0.295 0.295 560 32' 366 16,515 182 FAE 500 000 000 000 000 88,667 240 97,000 577 105,747 | -38,160 11,840 5 0.3786 3,239 9 232,848 Bft BOP 7 23,053 9 27,160 7 31,724 | 38,871.82 Discount 1.0000 0.9542 0.9105 | - 0.10 - | 1.0000 0.9000 0.9000 | - 194 - |
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| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2022 1/1/2022 1/1/2022 1/1/2022 1/1/2022 1/1/2027 1/1/2028 1/1/2029 1/1/2039 | Benefit Pa 21 Market Age v Actuarial Liability Normal Cost Age 39 400 411 422 433 444 45 466 477 488 49 50 | yments with Interest t Value of Assets | 3,5 249, 19, Salary 83,(85,(98,(108, 111,2 114,5 114,5 125,2 128,5 132,4 136,(140,5 145,2 149,4 149,4 | Termination 6 0.295 0.295 560 3.2' 366 16,513 182 FAE 000 0 000 0 000 0 555 114,611 000 111,272 555 114,611 020 118,044 358 121,593 326 125,236 311 128,999 316 132,866 143 136,857 1497 140,9557 | -38,160 11,840 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 232,848 9 242,498 9 342,498 9 35,607 5 5,4178 5 5,8461 1 62,951 7 67,659 7 7 67,659 7 7 67,659 7 7 67,659 7 7 7 7 7 7 7 7 7 7 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6858 0.6257 0.5971 | - 0.10 - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 | - 194 - - - - - - - - - - - - - - - 127 |
| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2020 1/1/2030 | Benefit Pa 21 Markei Age v Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 | yments with Interest t Value of Assets Service 13.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 25.00 | 3,5 249,5 19,7 Salary 83,0 85,0 98,0 108,0 108,0 111,2 114,4 118,0 121,5,2 125,2 128,0 132,1 136,4 140,0,145,5 149,4 149,4 153,5 | 2,9 Termination 6 0.295 560 322 560 322 560 16,515 182 FAE 000 000 500 500 500 500 500 50 | -38,160 11,840 5 0.3736 5 0.3736 3,239 3 232,848 Bft BOP 7 23,053 0 27,160 3 1,724 2 35,607 3 8,968 9 42,498 9 46,204 5 54,178 5 58,461 62,951 7 67,659 5 72,593 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6558 0.6257 0.5971 | - 0.10 - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 | - 194 - - - - - - - - - - |
| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2022 1/1/2022 1/1/2022 1/1/2023 1/1/2024 1/1/2025 1/1/2027 1/1/2028 1/1/2029 1/1/2039 | Benefit Pa 21 Markei Member 1 Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 500 51 52 | yments with Interest t Value of Assets Service Service 13.00 14.00 15.00 16.00 17.00 18.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 | 3,5 249, 19, Salary 83,(85,(98,(108, 111,2 114,5 114,5 125,2 128,5 132,4 136,(140,5 145,2 149,4 149,4 | Z,9 Termination 6 0.295 321 366 16,519 FAE 500 000 88,667 000 88,667 000 88,667 000 88,667 000 88,667 000 88,667 000 111,277 555 114,611 525 114,611 268 121,593 326 125,233 311 128,865 497 140,957 382 144,514 502 149,544 | -38,160 11,840 Retirement 5 0.3736 5 0.3736 5 0.3736 3,239 0 232,848 Bft BOP 7 23,053 0 27,160 31,724 2 35,607 38,968 0 42,498 0 46,204 8 50,095 5 54,178 5 58,461 62,951 7 67,659 7 77,761 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6858 0.6257 0.5971 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2018 1/1/2021 1/1/2022 1/1/2022 1/1/2023 1/1/2024 1/1/2026 1/1/2024 1/1/2026 1/1/2024 1/1/2026 1/1/2024 1/1/2026 1/1/2024 1/1/2035 1/1/2036 | Benefit Pa 21 Market Age v Actuarial Liability Normal Cost Age 39 400 411 422 433 444 45 466 47 48 49 500 511 52 533 54 | yments with Interest t Value of Assets | 3, 249, 19, <u>Salary</u> 83, 85, 98, 108, 111, 114, 114, 114, 125, 128, 132, 136, 132, 136, 149, 145, 149, 153, 158, 163, 168, | 2,9 Termination 6 0.295 560 3.22 366 16,515 182 FAE 500 500 500 577 105,747 555 114,617 500 577 105,747 555 114,617 555 114,617 568 121,590 568 121,590 568 121,590 568 121,590 568 121,590 579 140,957 301 128,982 311 128,982 314 133,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 143 138,865 144 145,185 502 149,547 502 | -38,160 11,840 5 6 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 27,160 7 31,724 235,607 38,968 9 42,498 9 46,204 8 5 5 5 5,417 6 5 5 5 5,417 6 7,7561 7,7561 7,7561 8 8,8431 7,7561 7,75 | Biscount Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6858 0.6257 0.5971 0.5436 0.5187 0.5436 | - 0.10 - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - 127 - - |
| 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2022 1/1/2022 1/1/2022 1/1/2023 1/1/2024 1/1/2028 1/1/2028 1/1/2033 1/1/2033 1/1/2034 | Benefit Pa 21 Market Age v Actuarial Liability Normal Cost Age 39 400 411 422 433 444 455 466 477 488 49 500 51 52 55 | yments with Interest t Value of Assets | 3,(249,(19,' Salary 83,(85,(98,(108,(111,2 114,(111,2 114,(114,(114,(114,(114,(125,2 128,(132,(136,(140,(145,(149,(153,(156,(168,2) 168,(173,(173,(173,(| 2,9 Termination 6 0.295 560 322 560 322 560 16,515 82 FAE 500 57 50 500 500 500 500 500 500 500 5 | -38,160 11,840 5 0.3736 5 0.3736 3,239 3 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 232,848 9 242,948 9 242, | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6587 0.6587 0.6587 0.6597 1.0.5697 0.5438 0.5187 0.4350 | - 0.10 | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2029 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2030 1/1/20 | Benefit Pa 21 Marke: Member 1 Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 56 56 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 15.00 14.00 15.00 16.00 17.00 18.00 17.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 25.00 26.00 27.00 28.00 28.00 29.00 30.00 | 3,(249, 19, <u>Salary</u> 83,(85,(98,(108,(111,2 114,5 114,5 125,2 128,(132,5 128,(133,6,1 140,(144,5,2) 136,1 153,1 158,(163,3 168,2 173,3 178,5 | Ze,9 Termination 6 0.295 321 366 16,519 FAE 500 000 88,667 000 88,667 000 88,667 000 88,667 000 88,667 000 88,667 000 111,272 555 114,611 525 114,611 1202 118,043 138 121,593 141 128,997 143 138,857 143 138,857 143 138,857 143 138,857 144,514 138,857 143 136,857 144,5143 136,857 145,159 144,5143 302 149,547 303 154,4027 304 154,4027 305 168,3005 | -38,160 11,840 Retirement 5 0.3736 5 0.3736 5 0.3736 3 239 9 232,848 BH BOP 7 23,053 9 27,160 2 31,724 2 35,607 3 8,968 9 42,498 9 46,204 8 50,095 5 54,178 5 58,461 6 62,951 7 67,659 7 77,761 7 83,175 8 88,843 9 47,766 1 00,986 9 100,986 9 100,986 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6558 0.6257 0.5971 0.5697 0.5436 0.5187 0.4507 | - 0.10 - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 20 | Benefit Pa 21 Market Member 1 Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 66 57 | yments with Interest t Value of Assets service Service 13.00 14.00 14.00 15.00 14.00 15.00 14.00 15.00 14.00 15.00 14.00 14.00 15.00 14.00 14.00 14.00 15.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 27.00 28.00 29.00 30.00 30.00 31.00 30.00 31.00 | 3, 249, 19, 52lary 83, 85, 98, 108, 111, 114, 114, 118, 125, 128, 132, 128, 132, 149, 149, 149, 149, 149, 149, 149, 149 | Termination 6 0.295 0.295 560 321 366 16,519 FAE 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 5111,427 555 514,611 525 514,614 555 514,614 136,857 516 132,868 143 136,857 362 145,184 502 144,514 502 158,644 308 163,400 508 168,401 508 168,403 508 168,403 508 163,403 508 163,403 508 163,403 508 163,403 508 163,403 | -38,160 11,840 5 0.3736 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,053 9 232,848 9 232,848 9 232,053 9 232,848 9 232,848 9 232,053 9 232,848 9 232,953 9 232,848 9 232,953 9 232,848 9 232,953 9 232,848 9 232,953 9 232,848 9 24,958 9 42,498 9 446,204 9 46,204 9 55,4178 9 55,4178 9 55,4178 9 55,4178 9 57,751 7 83,175 8 88,843 9 447,769 9 447,769 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7548 0.7242 0.6558 0.6257 0.6872 0.6872 0.6872 0.6558 0.6257 0.5971 0.5697 0.5436 0.5187 0.4507 0.4300 | - 0.10 | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2029 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2020 1/1/2030 1/1/20 | Benefit Pa 21 Market Member 1 Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 66 57 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 22.00 23.00 24.00 25.00 27.00 28.00 27.00 28.00 29.00 31.00 31.00 31.00 32.00 | 3,(249, 19, <u>Salary</u> 83,(85,(98,(108,(111,2 114,5 114,5 125,2 128,(132,5 128,(133,6,1 140,(144,5,2) 136,1 153,1 158,(163,3 168,2 173,3 178,5 | 2,9 Termination 6 0.255 660 3221 766 16,515 767 7 700 77 105,747 700 88,667 77 105,747 715 111,277 555 114,617 700 88,667 71 05,747 715 111,277 555 114,617 702 118,044 568 121,590 565 128,233 811 128,999 916 132,868 121,590 326 128,233 811 128,999 916 132,868 124,593 920 149,547 1300 158,648 308 168,307 308 168,307 309 178,560 309 178, | -38,160 11,840 Retirement 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 232,848 9 232,848 9 232,848 9 232,848 9 46,204 8 50,095 5 54,178 8 58,461 6 2,951 7 77,761 8 38,843 9 47,76 9 100,986 9 100,986 9 100,482 9 100,985 9 100,985 9 20,055 1 27,160 1 31,724 1 35,007 1 38,988 9 44,248 9 46,204 1 67,659 3 77,761 8 38,843 9 47,76 9 100,986 9 100,482 9 100,985 9 1 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6558 0.6257 0.5971 0.5697 0.5436 0.5187 0.4507 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 20 | Benefit Pa 21 Marke: Member 1 Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 46 55 56 56 56 56 56 56 56 56 5 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 14.00 15.00 20.00 20.00 20.00 20.00 20.00 20.00 21.00 22.00 23.00 24.00 24.00 25.00 26.00 27.00 28.00 28.00 29.00 30.00 31.00 33.00 30.00 33.00 30.00 | 3,(249, 19, 5alary 83,(85,(98,(108,(111,2 114,2 114,2 114,2 125,2 126,2 132,2 133,2 134,2 135,2 1 | Ze,9 Termination 6 0.295 321 366 16,519 FAE 500 500 321 500 322 560 322 566 16,519 560 322 560 322 577 505 500 500 500 500 500 500 500 500 500 111,272 555 114,611 505 114,611 522 118,043 535 12,593 511 12,865 522 143,543 502 149,543 502 149,543 503 154,027 526 158,464 508 168,300 508 168,300 508 168,303 509 173,355 379 178,560 500 | -38,160 11,840 Retirement 5 0.3736 5 0.3736 5 0.3736 3 239 9 232,848 BH BOP 7 23,053 9 232,848 BH BOP 7 23,053 9 27,160 3 1,724 2 35,607 3 8,968 9 42,498 9 46,204 8 50,095 5 54,178 8 58,461 6 2,951 7 67,659 9 72,593 9 77,761 7 83,175 8 88,843 9 44,776 9 100,986 9 107,482 9 114,278 9 12,385 128,815 128,8 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6558 0.6257 0.5971 0.5697 0.5436 0.517 0.4360 0.4103 0.4300 0.4103 0.4301 0.4301 0.4303 0.3915 0.3736 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 1.1.200 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2021 1/1/2022 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2033 1/1/2034 1/1/2035 1/1/2045 1/1/204 | Benefit Pa 21 Market Age V Actuarial Liability Normal Cost Age 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 00 00 61 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 14.00 15.00 14.00 15.00 14.00 15.00 14.00 14.00 15.00 14.00 15.00 14.00 15.00 16.00 17.00 18.00 20.00 21.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 25.00 26.00 26.00 27.00 28.00 29.00 30.00 31.00 33.00 34.00 34.00 34.00 34.00 34.00 34.00 34.00 35.00 | 3, 249, 19, 5alary 83, 83, 85, 98, 108, 111, 114, 114, 114, 114, 114, 125, 125, 128, 132, 132, 144, 144, 145, 149, 145, 149, 145, 149, 158, 168, 163, 173, 178, 183, 183, 193, 195, 195, 195, 195, 195, 195, 195, 195 | Termination 6 0.295 0.295 560 321 366 16,519 FAE 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 500 5114,611 525 114,613 555 114,613 568 121,593 511 111 526 124,593 516 132,864 526 145,514 502 145,514 502 145,544 503 158,643 504 163,400 505 163,401 508 168,3401 508 168,3401 508 168,3401 508 168,3401 508 168,3401 508 168,3401 | -38,160 11,840 5 0.3736 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 27,160 7 38,968 9 42,498 9 46,204 9 46,204 9 46,204 9 46,204 9 55,4,178 8 58,461 1 62,951 7 72,593 7 72,593 7 72,693 7 77,761 7 83,175 8 88,843 7 7,761 7 83,175 8 8,843 7 7,761 7 83,175 8 8,843 7 7,761 7 83,175 8 8,843 7 7,761 7 83,175 8 8,843 7 7,761 7 83,175 8 7,761 7 14,278 8 12,2845 7 13,662 7 13,675 7 14,278 7 14 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.5871 0.5897 0.5436 0.5187 0.4360 0.4723 0.4507 0.4300 0.4723 0.4507 0.4300 0.4507 0.3736 0.3736 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 1.1.202 ACTIVES Proj. Date 1/1/2018 1/1/2018 1/1/2022 1/1/2023 1/1/2023 1/1/2024 1/1/2025 1/1/2026 1/1/2026 1/1/2027 1/1/2028 1/1/2028 1/1/2028 1/1/2028 1/1/2038 1/1/204 | Benefit Pa 21 Market Age V Actuarial Liability Normal Cost Age 39 400 411 422 433 444 455 466 477 488 499 500 511 522 533 544 555 566 577 588 599 600 611 622 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 15.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 25.00 25.00 25.00 25.00 25.00 25.00 26.00 27.00 28.00 29.00 30.00 31.00 33.00 34.00 35.00 | 3, 249, 19, 5alary 83, 88, 98, 108, 111, 114, 114, 114, 114, 114, 114, 125, 128, 132, 136, 136, 136, 136, 136, 136, 136, 136 | Ze,9 Termination 6 0.295 0.237 366 16,513 182 FAE 000 88,667 000 000 000 000 000 88,667 101 111,272 555 114,611 102 118,044 368 121,593 371 128,998 311 128,998 313 136,857 314 136,857 302 1445,183 302 1445,183 302 144,9427 260 158,644 308 163,403 308 163,403 309 173,355 309 178,560 309 178,560 309 198,5117 312 189,433 3139 195,117 3147 200,970 | -38,160 11,840 5 5 0.3736 5 0.3736 3,239 9 232,848 Bft BOP 7 23,053 9 232,848 Bft BOP 7 23,053 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,053 9 232,848 9 232,053 9 237,160 7 38,968 9 44,2488 9 446,204 8 55,077 38,968 9 446,204 8 55,4178 8 58,461 62,951 7,7,761 7,7,761 7,7,761 8 38,843 9,477,659 3,77,765 8 8,88,843 9,477,659 3,77,761 100,986 9,107,482 9,107,482 9,107,482 100,985 100,985 100,985 100,985 100,985 100,985 114,278 121,385 122,355 123,557 124,557 126,557 127,557 126,557 126,557 126,557 126,557 127,557 126,577 126,577 126,577 126,577 126,577 126,577 | Biscount Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6858 0.6257 0.5971 0.5436 0.6187 0.5436 0.5187 0.5436 0.4300 0.4723 0.4300 0.4300 0.4300 0.4300 0.3366 0.3366 0.3366 0.3402 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.00000 0.0000000000 | - 194 - - - - - - - - - - - - - - - - - - - |
| 2020 E 2020 E 1.1.200 ACTIVES Proj. Date 1/1/2018 1/1/2019 1/1/2021 1/1/2022 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2023 1/1/2033 1/1/2034 1/1/2035 1/1/2045 1/1/204 | Benefit Pa 21 Markei Member 1 Age V Actuarial Liability Normal Cost Age 39 40 40 41 42 43 44 45 55 56 55 56 56 57 58 59 60 61 62 63 | yments with Interest t Value of Assets Service Service 13.00 14.00 14.00 15.00 16.00 17.00 18.00 19.00 20.00 21.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 24.00 22.00 23.00 24.00 22.00 23.00 24.00 24.00 25.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 26.00 27.00 28.00 29.00 29.00 20.00 20.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 27.00 26.00 27.00 28.00 29.00 29.00 20.00 20.00 21.00 22.00 23.00 24.00 25.00 26.00 27.00 26.00 27.00 28.00 28.00 29.00 29.00 20.00 27.00 28.00 29.00 20.00 27.00 28.00 29.00 29.00 20.00 | 3, 249, 19, 5alary 83, 83, 85, 98, 108, 111, 114, 114, 114, 114, 114, 125, 125, 128, 132, 132, 144, 144, 145, 149, 145, 149, 145, 149, 158, 168, 163, 173, 178, 183, 183, 193, 195, 195, 195, 195, 195, 195, 195, 195 | Termination 6 0.295 0.295 560 3.2' 566 16,513 57 16,513 500 500 500 500 577 105,747 555 114,611 500 125,238 511 125,238 511 125,238 511 125,238 511 125,238 512 144,611 502 144,518 502 144,518 502 144,518 503 149,543 504 158,644 505 163,303 506 168,303 507 175,566 508 163,303 509 168,301 509 168,303 509 168,301 501 164,303 502 158,643 503 173,556 504 168,303 505 <td< td=""><td>-38,160 11,840 5 0.3736 5 0.3736 8 232,848 Bft BOP 7 232,848 Bft BOP 7 233,053 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 42,498 9 44,499 9 44,499 9 44,498 9 44,499 9 44,499 9 44,499 9 44,498 9 44,498</td><td>38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.5871 0.5897 0.5436 0.5187 0.4360 0.4723 0.4507 0.4300 0.4723 0.4507 0.4300 0.4507 0.3736 0.3736</td><td>- - - - - - - - - - - - - - - - - - -</td><td>1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550</td><td>- 194 - - - - - - - - - - - - - - - - - - -</td></td<> | -38,160 11,840 5 0.3736 5 0.3736 8 232,848 Bft BOP 7 232,848 Bft BOP 7 233,053 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 232,848 9 42,498 9 44,499 9 44,499 9 44,498 9 44,499 9 44,499 9 44,499 9 44,498 9 44,498 | 38,871.82 Discount 1.0000 0.9542 0.9105 0.8688 0.8290 0.7910 0.7548 0.7202 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.6872 0.5871 0.5897 0.5436 0.5187 0.4360 0.4723 0.4507 0.4300 0.4723 0.4507 0.4300 0.4507 0.3736 0.3736 | - - - - - - - - - - - - - - - - - - - | 1.0000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.9000 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 0.8550 | - 194 - - - - - - - - - - - - - - - - - - - |

| ACTIVES | Member 2 | | | Termination | Retirement | | | | |
|------------|---------------------|---------|-----------|-------------|------------|----------|-----------|------------|-------|
| | Age | | | 65 | 60 | | | | |
| | v | | | 0.7202 | 0.9105 | | | | |
| | | | 2,828 | - | 2,828 | | | | |
| | Actuarial Liability | | 1,162,383 | - | 1,162,383 | | | | |
| | Normal Cost | | 38,111 | | | | | | |
| Proj. Date | Age | Service | Salary | FAE | Bft BOP | Discount | decrement | survival P | PUC |
| 1/1/2018 | | | 133,000 | | | | | | |
| 1/1/2019 | | | 135,000 | | | | | | |
| 1/1/2020 | | | 138,000 | | | | | | |
| 1/1/2021 | 58.00 | 30.50 | 141,000 | 135,333 | 82,553 | 1.0000 | - | 1.0000 | - |
| 1/1/2022 | 59 | 31.50 | 145,230 | 138,000 | 86,940 | 0.9542 | - | 1.0000 | - |
| 1/1/2023 | 60 | 32.50 | 149,587 | 141,410 | 91,917 | 0.9105 | 1.00 | 0.0000 | 2,828 |
| 1/1/2024 | 61 | 33.50 | 154,075 | 145,272 | 97,332 | 0.8688 | - | 0.0000 | - |
| 1/1/2025 | 62 | 34.50 | 158,697 | 149,630 | 103,245 | 0.8290 | - | 0.0000 | - |
| 1/1/2026 | 63 | 35.50 | 163,458 | 154,119 | 109,425 | 0.7910 | - | 0.0000 | - |
| 1/1/2027 | 64 | 36.50 | 168,361 | 158,743 | 115,882 | 0.7548 | - | 0.0000 | - |
| 1/1/2028 | 65 | 37.50 | 173,412 | 163,505 | 122,629 | 0.7202 | - | 0.0000 | - |

| INACTIVE | S | | | | | | |
|----------|----------|-----|---------|-----|----------|--------|---------|
| ID | Status | Age | Ann Bft | NRD | Discount | Factor | AL |
| 3 | Retired | 59 | 36,666 | 59 | 1.0000 | 15.10 | 553,657 |
| 4 | Deferred | 45 | 18,000 | 65 | 0.3915 | 13.40 | 94,439 |
| 5 | Retired | 61 | 24,000 | 61 | 1.0000 | 14.60 | 350,400 |
| 6 | Retired | 77 | 36,000 | 77 | 1.0000 | 9.20 | 331,200 |

CALCULATIONS FOR BENEFIT CHANGES

| MEMBEF | R 3 - ACTIVE TO RET | RED |
|--------|---------------------|---------|
| | FAE | 105,000 |
| | Svc | 18.00 |
| | Unreduced Benefit | 37,800 |
| | ERD | 3% |
| | Reduced Benefit | 36,666 |
| | | |
| MEMBEF | R 5 - DEFERRED TO I | RETIRED |
| | Unreduced Benefit | 24,000 |
| | ERD | 0% |
| | Reduced Benefit | 24,000 |

(b) Calculate the gains and losses on a going concern basis by source for 2020, excluding PfAD.

Commentary on Question:

This question was overall done poorly by candidates. Many candidates were able to successfully calculate some gain and loss items, however they left off key components and the gain and loss did not balance overall.

| Funding exc | cess (shortfall) at January 1, 2020, excluding PfAD | 96,000 |
|-------------|---|----------|
| | Sources | |
| | Interest on funding excess (shortfall) before PfAD | 4,800 |
| | Contributions in excess of accrual | 64,950 |
| | Investment return | 173,740 |
| | Salary | (8,346) |
| | Retirement | (81,557) |
| | Mortality | (6,000) |
| | Miscellaneous | (299) |
| | Impact of changes in assumptions | (72,893) |
| | | |
| | | |

| Funding excess (shortfall) at January 1, 2 | 021, excluding PfAD | | 170,396 |
|--|---------------------|-----------|---------------|
| | Liabilities | Assets | Gain / (Loss) |
| 1.1.2020 | 2,404,000 | 2,500,000 | 96,000 |
| Normal Cost/Employer Contribuions | 85,050 | 150,000 | 64,950 |
| Benefit Payments | (36,000) | (36,000) | - |
| Interest | 119,300 | 124,100 | 4,800 |
| Salary Experience | 8,346 | | (8,346) |
| Mortality Experience | 6,000 | | (6,000) |
| Retiement Expense | 81,557 | | (81,557) |
| Discount Rate Change | 72,893 | | (72,893) |
| Investment Return | | 173,740 | 173,740 |
| Misc | 299 | | (299) |
| 1.1.2021 | 2,741,444 | 2,911,840 | 170,396 |

| G/L by individual | Expected | Actual | | |
|-------------------|-------------|-------------|----------|-------------|
| - Mem1 | (219,450) | (234,659) | (15,209) | salary |
| - Mem2 | (1,141,350) | (1,134,487) | 6,863 | salary |
| - Mem3 | (543,900) | (542,657) | 1,243 | retirement |
| - Mem4 | (89,250) | (89,549) | (299) | misc - rour |
| - Mem5 | (260,400) | (343,200) | (82,800) | retirement |
| - Mem6 | (318,000) | (324,000) | (6,000) | mortality |
| Check | (2,572,350) | (2,668,552) | (96,202) | |

| ACTIVES | Member 1 | | | | | | | Terminat | tion | Retiren | nent | | | | | | |
|--|--|---|--|--|--|--|---|---|--|--|---|---|--|--|--|------------------|--|
| | Age | | | | | | | | 65 | | 60 | | | | | | |
| | v | | | | | | | | 0.2812 | | 0.3589 | | | | | | |
| | A | 1.194. | | | | | 3,560 | | 321 | | 3,239 | | | | | | |
| | Actuarial Lia Normal Cosi | | | | | | 234,659 18,051 | | 15,485 | | 219,174 | | | | | | |
| | Age | Service | | | | Salary | | FAE | | Bft BO | P [| Discount | | decrement | surviva | IP F | PUC |
| 1/1/2018 | | | | | | j | 83,000 | | | | | | | | | | |
| 1/1/2019 | | | | | | | 85,000 | | | | | | | | | | |
| 1/1/2020 | | | | | | | 98,000 | | | | | | | | | | |
| 1/1/2021 | | 39 40 | | | 13.00 14.00 | | 108,000 | | 88,667 | | 23,053 | | 1.0000 | - 0.10 | | 000 | - 194 |
| 1/1/2022 1/1/2023 | | 40 | | | 14.00 | | 111,240 114,577 | | 97,000 105,747 | | 27,160 31,724 | | 0.9524 | - 0.10 | 0.9 | 000 | - 194 |
| 1/1/2024 | | 42 | | | 16.00 | | 118,015 | | 111,272 | | 35,607 | | 0.8638 | - | | 000 | - |
| | | | | | | | | | | | | | | | | | |
| 1/1/2025 | | 43 | | | 17.00 | | 121,555 | | 114,611 | | 38,968 | | 0.8227 | - | | 000 | - |
| 1/1/2026 | | 44 | | | 18.00 | | 125,202 | | 118,049 | | 42,498 | | 0.7835 | | | 000 | - |
| 1/1/2027 1/1/2028 | | 45 46 | | | 19.00 20.00 | | 128,958 132,826 | | 121,590 125,238 | | 46,204 50,095 | | 0.7462 | - | | 000 | - |
| 1/1/2028 | | 40 | | | 20.00 | | 132,820 | | 125,236 | | 54,178 | | 0.6768 | | | 000 | - |
| 1/1/2030 | | 48 | | | 22.00 | | 140,916 | | 132,865 | | 58,461 | | 0.6446 | | | 000 | - |
| 1/1/2031 | | 49 | | | 23.00 | | 145,143 | | 136,851 | | 62,951 | | 0.6139 | | 0.9 | | - |
| 1/1/2032 | | 50 | | | 24.00 | | 149,497 | | 140,957 | | 67,659 | | 0.5847 | 0.05 | | 550 | 127 |
| 1/1/2033 | | 51 | | | 25.00 | | 153,982 | | 145,185 | | 72,593 | | 0.5568 | | | 550 | - |
| 1/1/2034 | | 52 | | | 26.00 | | 158,602 | | 149,541 | | 77,761 | | 0.5303 | | | 550 | - |
| 1/1/2035 1/1/2036 | | 53 54 | | | 27.00 28.00 | | 163,360 168,260 | | 154,027 158,648 | | 83,175 88,843 | | 0.5051 | - | | 550 550 | |
| 1/1/2036 | | 55 | | | 28.00 | | 173,308 | | 158,648 | | 94,776 | | 0.4610 | - | | 550 550 | |
| 1/1/2038 | | 56 | | | 30.00 | | 178,508 | | 168,309 | | 100,986 | | 0.4363 | | | 550 | - |
| 1/1/2039 | | 57 | | | 31.00 | | 183,863 | | 173,359 | | 107,482 | | 0.4155 | | 0.8 | | |
| 1/1/2040 | | 58 | | | 32.00 | | 189,379 | | 178,560 | | 114,278 | | 0.3957 | - | 0.8 | 550 | - |
| 1/1/2041 | | 59 | | | 33.00 | | 195,060 | | 183,916 | | 121,385 | | 0.3769 | | 0.8 | | - |
| 1/1/2042 | | 60 | | | 34.00 | | 200,912 | | 189,434 | | 128,815 | | 0.3589 | | | 000 | 3,239 |
| 1/1/2043 1/1/2044 | | 61 62 | | | 35.00 | | 206,939 | | 195,117 200,970 | | 136,582 | | 0.3418 | - | | 000 | - |
| 1/1/2044 | | 63 | | | 36.00 37.00 | | 213,147 219,542 | | 200,970 | | 144,699 153,180 | | 0.3256 | - | 0.0 | 000 | - |
| 1/1/2046 | | 64 | | | 38.00 | | 226,128 | | 213,209 | | 162,039 | | 0.2953 | | | 000 | |
| 1/1/2047 | | 65 | | | 39.00 | | 232,912 | | 219,606 | | 171,292 | | 0.2812 | - | | 000 | - |
| ACTIVES | Men | ber 2 | | | | | | | | | | | | | | | |
| | | | | | | | Termina | ation | Retirement | t | | | | | | | |
| | 100 | | | | _ | | Termina | | Retirement | _ | | | | | | | |
| | Age | | | | | | | 65 | | 60 | | | | | | | |
| | Age v | | | | | | | | | 60 | | | | | | | |
| | | | | | | 2,828 | | 65 | | 60 70 | | | | | | | |
| | V | | V | | | | | 65 .7107 | 0.90 2,82 | 60 70 28 | | | | | | | |
| | v Actu | arial Liabilit | y | | 1 | ,134,487 | | 65 .7107 - | 0.90 | 60 70 28 | | | | | | | |
| | v Actu Norr | | у | | | ,134,487 37,196 | 0 | 65 .7107 - | 0.90 2,82 1,134,48 | 60 70 28 37 | | | | | | | |
| Proj. Date | V Actu Norr Age | arial Liabilit | у | Service | 1. Sala | ,134,487 37,196 ary | | 65 .7107 - | 0.90 2,82 | 60 70 28 37 | iscount | decr | remen | t surviva | al P | PUC | 2 |
| Proj. Date 1/1/20 | V Actu Norr Age | arial Liabilit | у | Service | | ,134,487 37,196 | 0 | 65 .7107 - | 0.90 2,82 1,134,48 | 60 70 28 37 | iscount | decr | remen | t surviva | al P | PUC | 2 |
| | V Actu Norr Age | arial Liabilit | у | Service | | ,134,487 37,196 ary | 0 | 65 .7107 - | 0.90 2,82 1,134,48 | 60 70 28 37 | iscount | decr | remen | t surviva | al P | PUC | 2 |
| 1/1/20 | V Actu Norr Age 018 | arial Liabilit | У | Service | | ,134,487 37,196 ary 133,000 135,000 | 0 | 65 .7107 - | 0.90 2,82 1,134,48 | 60 70 28 37 | iscount | decr | remen | t surviva | al P | PUC | 2 |
| 1/1/20 1/1/20 1/1/20 | V Actu Norr Age 018 019 020 | arial Liabilit | | | Sala | ,134,487 37,196 ary 133,000 135,000 138,000 | FAE | 65 9.7107 - - | 0.90 2,82 1,134,48 Bft BOP | 60 70 28 37 Di | | | | | | PUC | > |
| 1/1/20 1/1/20 1/1/20 1/1/20 | v Actu Norr Age 018 019 020 021 | arial Liabilit | 58 | 30.5 | Sala | ,134,487 37,196 ary 133,000 135,000 138,000 141,000 | 0 FAE 135 | 65 .7107 - - 5,333 | 0.90 2,82 1,134,48 Bft BOP 82,55 | 60 70 28 37 Di 33 | 1.0000 |) | - | 1.0 | 0000 | PUC | - |
| 1/1/20 1/1/20 1/1/20 | v Actu Norr Age 018 019 020 021 | arial Liabilit | | | Sala | ,134,487 37,196 ary 133,000 135,000 138,000 | 0 FAE 135 | 65 9.7107 - - | 0.90 2,82 1,134,48 Bft BOP | 60 70 28 37 Di 33 | |) | | 1.0 | | PUC | |
| 1/1/20 1/1/20 1/1/20 1/1/20 | v Actu Norr Age 118 119 120 121 | arial Liabilit | 58 | 30.5 | Sala 0 | ,134,487 37,196 ary 133,000 135,000 138,000 141,000 | 0 FAE 135 | 65 .7107 - - 5,333 | 0.90 2,82 1,134,48 Bft BOP 82,55 | 60 70 88 37 57 Di 53 53 | 1.0000 | D 1 | - | 1.C 1.C | 0000 | | - |
| 1/1/20 1/1/20 1/1/20 1/1/20 1/1/20 1/1/20 | v Actu Norr Age 118 119 120 121 122 122 | arial Liabilit | 58 59 60 | 30.5 31.5 32.5 | 0 0 0 | ,134,487 37,196 ary 133,000 135,000 138,000 141,000 145,230 149,587 | 0 FAE 135 138 141 | 65 .7107 - - 5,333 3,000 I,410 | 0.90 2,82 1,134,48 Bft BOP 82,55 86,94 91,91 | 60 70 28 37 57 0 53 53 60 7 | 1.0000 0.9524 0.9070 |) 1 2 | - | 1.0 1.0 0.0 | 0000 | | - |
| 1/1/20 1/1/20 1/1/20 1/1/20 1/1/20 | v Actu Norr Age 118 119 120 121 122 122 | arial Liabilit | 58 59 | 30.5 31.5 | 0 0 0 | ,134,487 37,196 ary 133,000 135,000 138,000 141,000 145,230 | 0 FAE 135 138 141 | 65 .7107 - - 5,333 3,000 | 0.90 2,82 1,134,48 Bft BOP 82,55 86,94 | 60 70 28 37 57 0 53 53 60 7 | 1.0000 0.9524 |) 1 2 | - - 1.00 | 1.0 1.0 0.0 | 0000 | | - - 2,828 |
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(c) Calculate the solvency funded position as at January 1, 2021.

Commentary on Question:

Overall candidates did well on this part of the question. Note some candidates did not test for grow-in on the active members and some did not apply the new December 1, 2020 Commuted Value Standard.

| Net assets | 2,861,840 |
|---------------------------------------|-----------|
| Dresent value of account hanafits for | |
| Present value of accrued benefits for | • |
| Active members | 1,899,725 |
| Deferred pensioners | 216,000 |
| Pensioners | 1,659,253 |
| Total solvency liability | 3,774,977 |

Solvency excess (shortfall)

(913,137)

| MEMBER | 1 | 2 | 3 | 4 | 5 | 6 |
|--------------------|------------|-----------|---------|----------|---------|---------|
| Status | Active | Active | Retired | Deferred | Retired | Retired |
| Bft | 23,053 | 82,553 | 36,666 | 18,000 | 24,000 | 36,000 |
| Pts | 52 | 88.5 | | | | |
| Grow in? | FALSE | TRUE | | | | |
| SVC? | TRUE | TRUE | | | | |
| EURD | 65 | 60 | | | | |
| MAX | 10.60 | 20.30 | | | | |
| Opt Age | 65 | 58 | | | | |
| Age | w/ Red | w/ Red | | | | |
| 55 | 6.60 | - | | | | |
| 56 | 7.31 | - | | | | |
| 57 | 7.90 | - | | | | |
| 58 | 8.47 | 20.30 | | | | |
| 59 | 8.96 | 20.08 | | | | |
| 60 | 9.38 | 19.80 | | | | |
| 61 | 9.73 | 18.90 | | | | |
| 62 | 10.09 | 18.10 | | | | |
| 63 | 10.30 | 17.20 | | | | |
| 64 | 10.53 | 16.40 | | | | |
| 65 | 10.60 | 15.70 | | | | |
| Solvency Liability | 244,365.33 | 1,655,359 | 773,653 | 216,000 | 482,400 | 403,200 |

(d) Calculate the 1-year Solvency Incremental Cost.

Commentary on Question:

Overall this part of the question was done well by candidates. Many candidates struggled with discounting the projected actuarial liabilities.

| Solvency incremental cost | | (59,005) |
|---------------------------|-----------|-----------|
| Blended Solvency DR | 2.2% | |
| | 2021 | 2022 |
| Projected AL | 3,774,977 | 3,700,000 |
| AL at val date | 3,774,977 | 3,620,352 |
| Exp. Benefit | 95,620 | |
| SIC | (59,005) | |

(e) Calculate the minimum required and maximum permissible employer contributions for 2021 and the minimum required special payments for 2022.

Commentary on Question:

Many Candidates were able to correctly calculate the maximum contributions for 2021. Candidates struggled with determining the special payments with respect to both 2021 and 2022.

| Minimum required cont Minimum required spec Maximum permissible c | ial payments for 2022 | |
|---|-----------------------|------|
| | | 2021 |
| Normal cost | 57, | 293 |
| PfAD on normal cost | 5, | 729 |
| Special payments | | |
| Going Concern | 19, | 000 |
| Solvency | 274, | 825 |
| Minimum annual contribu | ution 356, | 848 |
| Maximum annual contrib | ution 976, | 160 |

| Prior amortization schedules | | | | 1/1/2021 | 1/1/2021 |
|------------------------------|---------------------------------------|------------------|----------------------|-----------|----------|
| Туре | Monthly Amortization Payment (\$000s) | Date Established | Date of Last Payment | Solv PV | GC PV |
| Going concern | 1,583 | 1/1/2021 | 12/31/2022 | 18,776 | 18,515 |
| Going concern | 939 | 1/1/2022 | 12/31/2031 | 53,290 | 85,234 |
| Solvency | 21,917 | 1/1/2021 | 12/31/2025 | 1,244,177 | |
| Solvency | 4,167 | 1/1/2020 | 12/31/2024 | 191,285 | |
| | | | | 1,507,527 | |

| Solvency assets | 2,911,840 | 2,911,840 |
|--|-----------|-----------|
| PV GC SP | 72,065 | 72,065 |
| PV Solv SP | 1,435,462 | - |
| Termination Expense | (50,000) | (50,000) |
| | | |
| Solvency liabilities | 3,774,977 | 3,774,977 |
| Reduced Solvency deficiency (85% ratio): | | 274.825 |

All solvency special payments cannot be eliminated but amortization period can be shortened so the reduced solvency excess moves to zero

(f) Develop the plausible adverse scenario disclosure as at January 1, 2021.

Commentary on Question:

This question was omitted or partially done by most candidates.

| | Going concern | | Deterioration of | |
|-------------------------------------|---------------|--------------------|-------------------------|----------------|
| | results | Interest rate risk | asset values | Longevity risk |
| Market value of assets | 2,911,840 | 3,028,314 | 2,693,452 | 2,911,840 |
| Going concern liability | 2,741,444 | 2,926,143 | 2,741,444 | 2,878,517 |
| PfAD | 274,144 | 292,614 | 274,144 | 287,852 |
| | | | | |
| Going concern funding target | 3,015,589 | 3,218,757 | 3,015,589 | 3,166,368 |
| Funding excess (shortfall) | (103,749) | (190,443) | (322,137) | (254,528) |
| Current service cost including PfAD | 63,022 | 68,751 | 63,022 | 66,173 |

| Interest Rate Risk | | |
|-------------------------------------|-----------|----------------------------|
| Duration of Asset Portfolio | 8.00 | |
| Fixed income allocation | 50% | |
| Market value of assets | 3,028,314 | =2,911,840*(1-8*-1%*0.5) |
| GC AL duration | 13.47 | |
| Going concern liability | 2,926,080 | =2,741,444*(1-13.47*-0.5%) |
| GC NC duration | 18.18 | |
| Current service cost | 62,501 | =57,293*(1-18.18*-0.5%) |
| Current service cost including PfAD | 68,751 | |

| Deterioration of asset values | | |
|-------------------------------------|-----------|------------------------|
| Market value of assets | 2,693,452 | =2,911,840*(1-0.5*15%) |
| Going concern liability | 2,741,444 | no change |
| Current service cost including PfAD | 63,022 | no change |

| Longevity risk | | |
|---|-----------|-------------------|
| Market value of assets | 2,911,840 | no change |
| Impact of longevity increase on AL & NC | 5% | |
| Going concern liability | 2,878,517 | =2,741,444*(1+5%) |
| Current service cost | 60,158 | =57,293*(1+5%) |
| Current service cost including PfAD | 66,173 | |

- 2. The candidate will understand how to analyze/synthesize the factors that go into selection of actuarial assumptions for funding purposes.
- 7. The candidate will understand how to apply the standards of practice and professional conduct guidelines.

Learning Outcomes:

- (2a) Describe and apply the techniques used in the development of economic assumptions for funding purposes.
- (2b) Evaluate and recommend appropriate assumptions for funding purposes.
- (2c) Evaluate actual experience, including comparisons to assumptions.
- (7d) Demonstrate compliance with requirements regarding the actuary's responsibilities to the participants, plans sponsors, etc.
- (7e) Explain and apply all of the applicable standards of practice related to valuing pension benefits.
- (7f) Recognize situations and actions that violate or compromise Standards or Professional Conduct Guidelines.

Sources:

ASOP 35: Selection of Demographic and Other Noneconomic Assumptions for Measuring Pension Obligations

CIA Rules of Professional Conduct

Commentary on Question:

The question was not answered well by most of the candidates. Most candidates did not refer to any specific standards of practice in part b) and lost points. Many candidates also did not describe why the assumptions do not meet the standards.

Solution:

(a) Describe the considerations for setting a retirement rates assumption.

The actuary should take into account factors such as the following:

- employer-specific or job-related factors such as occupation, employment policies, work environment, unionization, hazardous conditions, and location of employment;
- the plan design, where specific incentives may influence when participants retire;
- the design of, and anticipated payment from, social insurance programs (for example, Social Security or Medicare); and

• the availability of other employer-sponsored postretirement benefit programs (for example, postretirement health coverage or savings plan).

The actuary should also consider:

- Materiality The actuary should take into account the balance between refined demographic assumptions and materiality (the actuary should use professional judgement if the use of more refined assumptions is not expected to produce materially different results).
- Cost of Using Refined Assumptions The actuary should take into account the balance between refined demographic assumptions and the cost of using refined demographic assumptions.
- Combined Effect of Assumptions The combined effect of all nonprescribed assumptions selected by the actuary (both demographic assumptions selected in accordance with this standard and economic assumptions selected in accordance with ASOP No. 27) should be reasonable. For example, the actuary may have decided not to make any assumption with regard to four different types of future events, each of which alone is immaterial. However, the effect of omitting assumptions for all four types of future events may be a material understatement or overstatement of the measurement results.
- Changes in circumstance The demographic assumptions selected should reflect the actuary's knowledge as of the measurement date. However, the actuary may learn of an event occurring after the measurement date, that would have changed the actuary's selection of a demographic assumption. If appropriate, the actuary may reflect this change as a subsequent event as of the measurement date.
- Views of experts Demographic data and analyses are available from a variety of sources, including representatives of the plan sponsor and administrator, demographers, economists, and other professionals. When the actuary is responsible for selecting or giving advice on selecting demographic assumptions within the scope of this standard, the actuary may incorporate the views of experts, but the selection or advice should reflect the actuary's professional judgment.

(b) You are the actuary for a plan with the following provisions:

| Normal Retirement Age: | 65 |
|----------------------------|---|
| Normal Retirement Benefit: | Monthly benefit of \$60 per year of credited service |
| Earliest Retirement Age: | 55 |
| | Unreduced at Age 60 |
| Early Retirement Benefit: | Reduced by 3% for each year by which retirement precedes age 60 |
| Bridge Benefit: | Monthly benefit of \$20 per year of credited service |
| | Payable from Early Retirement Age to Age 65 |

The company that sponsors the plan has asked you to use the following retirement assumption:

| Age | Probability of Retirement |
|-----|----------------------------------|
| 62 | 50% |
| 65 | 100% |

Critique the company's proposed retirement assumption, referencing the applicable professional standards.

The professional standards that apply to this situation are:

- Rule 1 Professional integrity. A member shall act honestly, with integrity and competence, and in a manner to fulfil the profession's responsibility to the public and to uphold the reputation of the actuarial profession.
- Rule 3 Standards of Practice. A member shall ensure that professional services performed by or under the direction of the member meet applicable standards of practice.
- Rule 6 Control of work product. A member who performs professional services shall take reasonable steps to ensure that such services are not used to mislead other parties or to violate or evade the law.

In general the retirement assumption should:

- reflect the actuary's professional judgment.
- take into account actual plan experience relevant as of the measurement date but would not necessarily have to reflect current conditions persisting into the future.

• reflect the actuary's estimate of future experience, the actuary's observation of the estimates inherent in market data, or a combination thereof.

In particular, with respect to the company's proposed retirement assumption:

- May not be appropriate to change to a retirement age of 65 when members are entitled to unreduced pension at 60 with a bridge benefit
- The Company's proposed assumption would contravene Rule 3 since the assumption would not be "reasonable".
- Rule 6 would be violated by an inappropriate retirement age assumption as it may understate the liabilities

5. The candidate will understand how to evaluate and apply regulatory policies and restrictions for registered retirement plans.

Learning Outcomes:

- (5c) The candidate will be able to describe and apply regulation pertaining to plan amendment.
- (5h) The candidate will be able to describe and apply regulation pertaining to members' rights.
- (5i) The candidate will be able to describe and apply regulation pertaining to contributions and benefits.

Sources:

Canadian Pensions and Retirement Income Planning, Willis Towers Watson - Chpt. 17

Commentary on Question:

Part A was generally not well answered. It was apparent most candidates had not read this particular study not as they were not able to describe the requirements under the CRA for a special downsizing program or the additional benefits that may be granted under such a program.

Candidates did much better on part b, and generally understood what ancillary benefits could be changed, and to what extent under the ITA, to improve the value of benefits without generating a PSPA.

Solution:

(a) Describe the CRA's special downsizing program requirements and the additional benefits that may be provided.

CRA's special downsizing program requirements :

- Program must result in a net reduction of the greater of 50 employees or 10% of employees
- Reduction must be met within 2 years (i.e. program cannot span more than 2 years)
- Benefits under the program must commence within two years of program approval
- The program must me non-discriminatory -> benefit improvements cannot favor high-paid employees
- Targeted group may consist of no more than 35% in top earnings quartile
- No employees within the targeted group may continue to provide services to the company

• Any additional benefit under the downsizing program must not be paid as a lump-sum

Additional benefit that can be offered under a downsizing program:

- Eligibility: Members aged 55 and over at termination
- Additional service: lesser of 7 years number of years from termination date to age 65
- Accrual Rate: **for additional service described** above, lesser of the maximum pension under the Income Tax Act (ITA) in the year of termination and 2% of the member's Final 3-year Average Earnings
- Indexation: additional benefit as determined above indexed at 100% of CPI
- Unreduced benefits at the lesser of 25 years of service; or age 55; or 75 points, and reduced 3% per year to the above
- (b) Recommend changes to the provisions that meet the client's goals but do not require the approval of a special downsizing program.

Current provisions can be amended to enhance benefits which do not create a PSPA and do not require qualifying for a special downsizing program are:

- Enhancing the early retirement reduction– unreduced retirement at earlier of age 60, 30 years of service or 80 points
- Enhance the Plan's FAE to FAE3
- Provide post retirement indexation of up to 100% of CPI
- Enhance the normal form of payment
 - Single: life and guaranteed for 180 payments
 - $\circ~$ Married: Joint and survivor 66 and 2/3 guarantee for 5 year
- Offer a bridge benefit– up to CPP plus OAS

- 3. The candidate will understand how to apply/synthesize the methods used to value pension benefits for various purposes.
- 5. The candidate will understand how to evaluate and apply regulatory policies and restrictions for registered retirement plans.

Learning Outcomes:

- (3b) Perform periodic valuations of ongoing plans, calculating normal cost and actuarial liability, using a variety of cost methods.
- (5h) The candidate will be able to describe and apply regulation pertaining to members' rights.

Sources:

Pension Mathematics for Actuaries (Anderson)

FR-132-17 Chapter 5 of A Problem-Solving Approach to Pension Funding and Valuation, Second Edition

Commentary on Question:

Parts a) and b) were answered well by candidates that were familiar with the cost method. Some candidates were not familiar with the cost method and did poorly as a result. Almost all candidates were not able to determine the gain/loss in part c) and as a result scored poorly in this part.

Solution:

(a) Calculate the unfunded actuarial liability and the total normal cost as at January 1, 2021.

Show all work.

| AAN UAL _{initial} AAN NC _t | = UC UAL _{initial} = $(\sum PVFB_t - AL_t) / \sum PVFY_t \ge n$ |
|---|--|
| AANINC | $-(\underline{\sum} \mathbf{I} \mathbf{V} \mathbf{I} \mathbf{D}_t - \mathbf{A} \mathbf{L}_t) / \underline{\sum} \mathbf{I} \mathbf{V} \mathbf{I} \mathbf{I}_t \mathbf{X} \mathbf{I}$ |
| Member A | |
| PVFB | $= 100 \times 12 \times (60-30) \times \ddot{a}_{60}^{(12)} \times v^{(60-43)} \times .95^{2} +$ |
| | $100 	imes 12 	imes 13 	imes {\ddot{a}_{60}}^{(12)} 	imes v^{(60-43)} \ x \; .05 \; +$ |
| | $100 \times 12 \times 14 \times \ddot{a}_{60}^{(12)} \times v^{(60-43)} x$.95 x.05 |
| | $= 1200 \times 30 \times 14.8 \times .4363 \text{ x} .95^2 +$ |
| | $1200 \times 13 \times 14.8 \times .4363 \text{ x } .05 +$ |
| | $1200 \times 14 \times 14.8 \times .4363 \text{ x} .95 \text{ x} .05$ |
| | = 219,983 |
| PVFY | $= .95 + .95^2 / 1.05 \text{ x } \ddot{a}_{60-44}$ |
| | $= .95 + .95^2 / 1.05 \times 11.3797$ |
| | = 10.7311 |

| UC AL | = 1200 × 13 × 14.8 × .4363 = 100,732 | |
|---|---|-------------------------------------|
| <u>Member B</u> PVFB PVFY UC AL | $= 100 \times 12 \times (60-35) \times \ddot{a}_{60}{}^{(12)} \times v{}^{(60-5)}$ = 1200 × 25 × 14.8 × .61391 = 272, = \ddot{a}_{60-50}] = 1200 × 15 × $\ddot{a}_{60}{}^{(12)} \times v{}^{(60-50)}$ = 1200 × 15 × 14.8 × .61391 = 163, | 577 = 8.1078 |
| <u>Member C</u> PVFB PVFY UC AL | $= 100 \times 12 \times (60-40) \times \ddot{a}_{60}{}^{(12)} \times v{}^{(60-5)}$ = 1200 × 20 × 14.8 × .95238 = 338, = \ddot{a}_{60-59}] = 1200 × 19 × $\ddot{a}_{60}{}^{(12)} \times v{}^{(60-59)}$ = 1200 × 19 × 14.8 × .95238 = 321, | 286 = 1 |
| $\sum PVFB_{2021}$ $\sum PVFY_{2021}$ UC AL ₂₀₂₁ | = 219,983 + 272,577 + 338,286 = 10.7311 + 8.1078 + 1 = 100,732 + 163,546 + 321,371 | = 830,846 = 19.8389 = 585,649 |
| AAN UAL ₂₀₂ | | = 585,649 |

| AAN NC2021 | $= \left(\sum PVFB_{2021} - AL_{2021}\right) / \sum PVFY_t \ x \ n$ |
|------------|---|
| | = (830,846 – 585,649) / 19.8389 x 3 |
| | = 37,078 |

(b) Calculate the unfunded actuarial liability and the total normal cost as at January 1, 2022.

Show all work.

$$\begin{array}{ll} \underline{\text{Member A}} \\ \hline \text{PVFB} \end{array} &= 100 \times 12 \times (60\text{-}30) \times \ddot{a}_{60}{}^{(12)} \times v^{(60\text{-}44)} \text{ x } .95 + \\ & 100 \times 12 \times 14 \times \ddot{a}_{60}{}^{(12)} \times v^{(60\text{-}44)} \text{ x } .05 \end{array} \\ &= 1200 \times 30 \times 14.8 \times .4581 \text{ x } .95 + \\ & 1200 \times 13 \times 14.8 \times .4581 \text{ x } .05 \end{array} \\ &= 237,573 \end{array}$$

| PVFY | $= .95 \text{ x } \ddot{a}_{60-44} \rceil$ = .95 x 11.3797 | = 10.8107 |
|---|--|------------------------|
| <u>Member B</u> PVFB | $= 100 \times 12 \times (60-35) \times \ddot{a}_{60}^{(12)} \times v^{(60-51)}$ | |
| PVFY | = $1200 \times 25 \times 14.8 \times .6446$ = \ddot{a}_{60-51} | = 286,206 = 7.4632 |
| <u>Member C</u> PVFB | $= 100 \times 12 \times (61\text{-}40) \times \ddot{a}_{60}^{(12)} \times v^{(60)}$ $= 1200 \times 21 \times 14.5 \times .95238 = 348$ | ,000 |
| PVFY | $=\ddot{a}_{60-59}$ | = 1 |
| $\frac{\sum PVFB_{2022}}{\sum PVFY_{2022}}$ | = 237,573 + 286,206 + 348,000 = 10.8107 + 7.4632 +1 | = 871,779 = 19.2739 |
| F ₂₀₂₂ | = 150,000 *1.0 = 150,000 | |
| AAN UAL ₂₀₂₂ = Expected AAN AL ₂₀₂₂ = (AAN AL ₂₀₂₁ + AAN NC ₂₀₂₁) x 1.05 – 2021 Contributions w/int = (585,649 + 37,078) x 1.05 – 150,000 x 1.0 = 503,864 | | |
| AAN AL ₂₀₂₂ | $= AAN UAL_{2022} + F_{2022} \\= 503,864 + 150,000$ | = 653,864 |
| AAN NC2022 | $= (\sum PVFB_{2022} - AL_{2022}) / \sum_{= (871,779 - 653,864) / 19.2}$ = 33,919 | |
| Coloulate the impact of democraphic experience, by source, between January 1 | | |

(c) Calculate the impact of demographic experience, by source, between January 1, 2021 and January 1, 2022, on the normal cost **per active member**.

Show all work.

| Increase in per member normal cost due to termination experience (Member A): | | |
|--|---|--|
| Exp'd PVFB ₂₀₂₂ | = 219,983 x 1.05 = 230,982 | |
| Act'l PVFB ₂₀₂₂ | = 237,573 | |
| Exp'd PVFY ₂₀₂₂ | $= .95^2 \text{ x } \ddot{a}_{60-44} = 10.2702$ | |
| Act'l PVFY ₂₀₂₂ | = 10.8107 | |
| Exp'd NC ₂₀₂₂ | = (871,779 + (230,982 - 237,573) - 653,864) / | |
| | (19.2739 + (10.2702 - 10.8107)) | |
| | = 211,324 / 18.7334 = 11,281 | |

| Act'l NC ₂₀₂₂ per mbr | = 33,919 / 3 = 11,306 | | |
|---|--------------------------------------|--|--|
| Experience Loss | = 11,306 - 11,281 = 25 | | |
| 1 | | | |
| Decrease in per member normal cost due to retirement experience (Member C): | | | |
| Exp'd PVFB ₂₀₂₂ | = 338,286 x 1.05 = 355,200 | | |
| Act'l PVFB ₂₀₂₂ | = 348,000 | | |
| Exp'd PVFY ₂₀₂₂ | = 0 (assumed to retire) | | |
| Act'l PVFY ₂₀₂₂ | = 1 (assumed to retire 1 year later) | | |
| Exp'd NC ₂₀₂₂ | = (211,324 + (355,200 - 348,000)) / | | |
| | (18.7334 + (0 - 1)) | | |
| | = 12,323 | | |
| NC (incl term'n exp) | = 11,281 | | |
| Experience Gain | = 12,323 - 11,281 = 1,042 | | |
| | | | |

4. The candidate will understand the principles and rationale behind regulation.

Learning Outcomes:

- (4a) Describe the principles and motivations behind pension legislation and regulation.
- (4b) Describe sources and framework of government regulation.

Sources:

FR-139-18: OECD Core Principles of Private Pension Regulation

Ontario Pension Benefit Act

Commentary on Question:

Many candidates had difficulty answering this question. In particular, many candidates could only identify some points related to the PBA, but few candidates listed points related to Core Principle 7.

Solution:

Compare and contrast the principles set out in Core Principle 7 of the OECD Core Principles of Private Regulations against the established framework for defined benefit pension plans regulated by the Pension Benefits Act (Ontario) and the Income Tax Act (Canada) for the following:

- (i) Measurement of pension plan liabilities;
- (ii) Funding requirements of pension plans, and the treatment of surpluses or deficits; and
- (iii) Wind-up or termination of pension plans.
- (i) Measurement of pension plan liabilities;
 - Core Principle 7:
 - The plan's liabilities be calculated at least once every three years by an actuary or an equivalent specialist with required competency in pension.
 - A certification or report of the adjusted development of the liability and changes in risks covered is required for the intervening years.
 - The ongoing liability should take into account the projected benefits to be received with plan eligibility and vesting requirement met at the time of retirement, mortality and withdrawal decrements.
 - The termination liability should reflect the pension benefits payable if the plan terminates at the time of the valuation with the accrual of further entitlement ceased.

- The termination liability equals the cost of the benefits payable at the time the plan winds up, such as the cost of purchasing annuities or payment of lump sums, plus the cost of termination.
- Both ongoing and termination liability should reflect benefit indexation factors prescribed by law or the plan terms.
- Takes into account liabilities over time in relation to current and future years (ongoing liability) to assure that pension assets match this potential ongoing liability as it accrues and matures over time.
- Requires that the calculation method includes a prudent funding method, amortization rules and demographic, behavioral and economic assumptions that are considered appropriate and consistent with the generally required recognized actuarial standards.
- The use of prudent discount rates for determining the ongoing and termination liabilities, which are consistent with market conditions and are compatible with the methodologies used in the valuation of assets and other economic assumptions.
- Legal provision or actuary profession should provide guidance on the discount rate and assumption setting.
- Allows additional level of prudence if using established methods creates an unacceptable risk to member benefits.
- PBA/ITA:
 - Actuary prepares triennial actuarial valuations using methods and actuarial assumptions that are consistent with accepted actuarial practice. Plans less than 85% funded on solvency basis requires annual actuarial valuation. A cost of certificate is required for the intervening year when plan is applying surplus for contribution holiday.
 - The valuation must be completed both on a solvency basis, under which assets and liabilities are valued as if the plan is terminated on the date of the valuation, and on a going concern basis, under which valuation proceeds on the assumption that the plan will continue indefinitely.
 - There is no statutory compulsion to provide inflation protection in the form of indexing (ad hoc indexing is more common for private sector defined benefit plan).
 - Requires the provision of adverse deviation (PfAD) in the going concern liability to create an explicit funding cushion, but at a lower required funding level under solvency.
 - A solvency deficiency can be amortized over a five-year period, while a going concern unfunded liability can be amortized over a 10-year period.
 - Going concern assumptions are selected by actuary while solvency assumptions are largely prescribed based on the market conditions on valuation date.

- (ii) Funding requirements of pension plans, and the treatment of surpluses or deficits; and
 - Pension plans are required to maintain a level of assets that equal to the target funding level after factoring the operational plan cost.
 - The legal separation of pension plan assets should be mandatory as a minimum level of protection for the pension assets. Pension plan should be funded through the establishment of a pension fund.
 - Plan sponsors should be subject to minimum funding rules or other mechanisms to ensure adequate funding of pension liabilities. The pension fund is usually held by a trust company or insurance company.
 - PBA/ITA:
 - Must be funded; the plan's assets must be sufficient to pay for its going concern deficiency up to 100% of the liability, and fund solvency deficiency up to 85% of solvency liabilities through special payments.
 - Sets permissible benefits, maximums on tax-deductible contributions, and maximum limits on pension amounts.
 - Contributions and investment earnings for registered pension plans are tax-exempt until such time as benefits commence to be paid.
 - Surplus can be applied toward required employer/member contributions, provided that the plan remains fully funded on a going concern basis and maintains a transfer ratio of at least 105%. Surplus above this level is considered "available actuarial surplus" and can be used to allow employers to take a contribution holiday.
 - A solvency deficiency can be amortized over a five-year period, while a going concern unfunded liability can be amortized over a 10-year period.
 - Core Principle 7:
 - Allows for flexibility in the targeted funding level, which may be based on the termination liabilities or the ongoing liabilities.
 - The funding target should balance the need for benefit security and the affordability of the pension provision; should take account of the plan sponsor's ability to increase contribution and the possibility of adjusting benefit provisions in the case of underfunding.
 - Tax regulations should not discourage the build-up of sufficient reserves to withstand adverse market conditions and should avoid restricting the full funding, but does not have specific restrictions on minimum or maximum contribution levels.
 - Temporary suspension of contribution obligations, benefit increases, or a return of the surplus to the plan sponsor should only be permitted in circumstances of high levels of overfunding
 - The approved funding method for the ongoing liability may reduce volatility in the funding contribution level by spreading the funding of the liability over the expected working life of plan members.

- Acceptable mechanism and recovery periods for correcting situations of over or underfunding should be in place and provide incentives to build reserves against future market downturns.
- Contributions should cover the normal costs and allow prudent amortization of supplemental costs over time to achieve a smoother contribution schedule and more stable funding levels.
- Allows flexibility for the temporary limited under-funding and overfunding. Structural underfunding should be prohibited.
- (iii) Wind-up or termination of pension plans.
 - Core Principle 7 defines wind-up as a plan that is terminated or when the plan's obligation to pay benefits to members and beneficiaries is extinguished.
 - The allocation of the plan assets and the responsibility for underfunding should be clearly established in the event of windup.
 - When assets exceed liabilities, there should be rules to determine the allocation of the funding surplus; when assets are insufficient to cover benefit obligation, there should be rules to determine the allocation of the benefit payment.
 - Creditor rights of pension plan members and beneficiaries should be recognized in the case of bankruptcy of the plan sponsor or pension fund.
 - Legal provisions should be put in place to ensure that employee contributions owed to the plan are paid in the event of insolvency or at least has priority rights relative to other creditors.
 - Vested entitlement should be protected from creditors by the legal separation of plan assets.
 - PBA defines wind-up as the termination of a pension plan and the distribution of plan assets.
 - On a wind-up, benefits of all employees become immediately vested and the portability rights available in the case of the termination of employment of an individual who is not entitled to an immediate pension may be exercised by any employee who is entitled to a benefit.
 - If the valuation shows that the assets of the plan are more than sufficient to cover liabilities (including employees' wind-up rights), the resulting surplus in the plan will be distributed. If the plan does not address how surplus is to be distributed on wind-up, it must be distributed proportionately.
 - If the valuation shows that the plan is in a deficit position, the employer is obliged to pay into the plan the amount necessary to ensure that the pension entitlements under the plan will be paid. In the case where an employer is insolvent and not able to make the payment required, subject to the payment from the Pension Benefits Guarantee Fund, the PBA requires that the plan benefits be reduced in proportion to the wind-up deficiency.

- The Pension Benefits Guarantee Fund provides protection of the pension benefits of Ontario employees who are members of defined benefit pension plans registered under the PBA, subject to certain exceptions and limits.
- If a pension plan provides enhanced early retirement benefits, the PBA allows older or long-service members who meet "rule of 55" to "grow in" to the enhanced early retirement benefits they would have received if their plan had not been wound up.

2. The candidate will understand how to analyze/synthesize the factors that go into selection of actuarial assumptions for funding purposes.

Learning Outcomes:

- (2a) Describe and apply the techniques used in the development of economic assumptions for funding purposes.
- (2b) Evaluate and recommend appropriate assumptions for funding purposes.

Sources:

Provisions for Adverse Deviations in Going Concern Actuarial Valuations,

A Practical Approach to Establishing Margins for Adverse Deviations in Going Concern Funding Valuations

FR-144-20: FSRA - Frequently Asked Questions Pertaining to the 2018 Funding Reform for Defined Benefit Pension Plans

Determination of Best Estimate Discount Rates for Going Concern Funding Valuations, CIA Educational Note, Dec 2015

Commentary on Question:

Commentary listed underneath question component.

Solution:

(a) Describe the considerations for setting the best estimate going concern discount rate.

Commentary on Question:

Generally, most candidates were able to provide information on the most common approaches used to determine a best estimate going concern discount rate.

There are two typical approaches to setting a best estimate going concern discount rate:

- 1. Building block approach
 - a. Determine the best estimate of long-term, expected future investment returns for various asset classes
 - b. Combining best estimate long-term, expected future investment returns for different asset classes to reflect a plan's investment policy
 - c. With consideration for effects of diversification and rebalancing
 - d. Considering inclusion of an allowance for additional return due to active vs passive management
 - e. Making appropriate provision for expenses

- 2. Based on fixed income yields
 - a. Where an immunized portfolio is established to match projected cash flows, appropriate to base the discount rate assumption on the yield of the immunized portfolio
 - b. The asset mix has no impact on the setting of the discount rate in this approach
- (b) Recommend an approach for establishing the margin on the going concern discount rate.

Commentary on Question:

The candidates who did well on this question clearly stated a recommendation of how to establish a margin, and provided details on its development. Many candidates did not provide either a clear recommendation and/or enough information on how it would be developed.

There are a number of approaches on how to establish a margin on the going concern discount rate. Three potential approaches are outlined below but there may be other ways that could be considered a reasonable answer if enough detail is provided.

Sample Approach 1

- Recommendation: Incorporate PfAD in accordance with ON pension legislation (or similar)
- Determine whether closed or open plan and apply associated amount (with ON pension legislation or other reasonable amount provided)
- Determine proportion of fixed income and non-fixed income assets based on investment policy and regulations, apply associated amount (with ON pension legislation or other reasonable amount provided)
- If discount rate exceeds benchmark, apply associated amount (with ON pension legislation benchmark or other reasonable amount provided)

Sample Approach 2

- Recommendation: Using a building block approach incorporating margins within the components of a going concern discount rate
- Determine a risk-free rate using historical 10 year GoC bond yields
- Equity risk premium, start with best estimate and adjust downwards based on maturity of plan with larger margin for mature plans
- Incorporate margin for fixed-income risk premium
- Diversification & rebalancing: best estimate of 0.5% and reduced for margin
- Assume no added return from active management

Sample Approach 3

- Recommendation: Incorporate explicit margin based on plan characteristics
- Plan's Investment policy: margin is higher for plans that adopt a riskier investment policy. The higher the proportion of pension fund invested in nonfixed income assets, the higher the discount rate margin required
- Plan maturity: margin higher for mature plans than for less mature plans
- Current level of long-term interest rates: it moves with long-term interest rates that fall within a specified range—a higher (lower) margin is applied when interest rates move up (down)

5. The candidate will understand how to evaluate and apply regulatory policies and restrictions for registered retirement plans.

Learning Outcomes:

- (5a) The candidate will be able to describe and apply regulation pertaining to plan design.
- (5h) The candidate will be able to describe and apply regulation pertaining to members' rights.

Sources:

Canada Revenue Agency PA Guide

Canadian Pensions and Retirement Income Planning, Willis Towers Watson, 6th Edition, 2017 - Chpt 22

Commentary on Question:

The question was answered well by most of the candidates. However, some students did not apply the correct PA formula when dealing with two benefit periods/employers.

Solution:

Calculate the total 2021 Pension Adjustment for each member from all employers.

Show all work.

<u>Member A</u>

2021 PA formula = (9 x 2021 DB accrual) – 600

PA calculation for January 1st to June 30th

Service = 0.5 year.

Pension Plan Accrual = [1.0% x \$61,600 + 1.5% (\$250,000-\$61,600)] x 0.5

 $= [\$616 + \$2,826] \times 0.5 = \$1,721$

ITA Maximum Accrual = \$3,245.56 x 0.5 = \$1,622.78

PA (January 1 to June 30) = 9 x min (\$1,721, \$1,622.78) - 600 = **\$14,005**

PA calculation for September 30th to December 31st

Service = 0.25 year.

2021 Pension Plan Accrual = [1.0% x \$61,600 + 1.5% (\$250,000-\$61,600)] x 0.25

= [\$616 + \$2,826] x 0.25 = \$860.50

ITA Maximum Accrual = \$3,245.56 x 0.25 = \$811.39

PA (September 30th to December 31st) = $9 \times \min(\$860.50, \$811.39) - 600 = \$6,703$

Total 2021 PA = \$14,005 + \$6,703 = \$20,708

Member B

2021 PA formula = (9 x 2021 DB accrual) – 600

- 2021 service = 1 year. Since member accrued service while disabled, a full year service used for PA.
- Since member's service was restated before April 30, 2022, a corrected PA will be filed (not a PSPA)

2021 Pension Plan Accrual = [1.0% x \$61,600 + 1.5% (\$110,000-\$61,600)] x 1

=\$616 + \$726 = \$1,342

ITA Maximum Accrual = \$3,245.56

2021 PA = 9 x min (\$1,342, \$3,245.56) - 600 = \$11,478

Member C

2021 PA formula = (9 x 2021 DB accrual) – 600

PA under first employer

Service: 7/12 = 0.5833

2021 Pension Plan Accrual = [1.0% x \$61,600 + 1.5% (\$130,000- \$61,600)] x 0.5833

= [\$616 + \$1,026] x 0.5833

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= $957.78
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ITA Maximum Accrual = \$3,245.56 x 0.5833 = \$1,893.14

2021 PA = 9 x min (\$957.78, \$1,893.14) – 600 = \$8,020

PA under second employer

Service: 5/12 = 0.4167

2021 Pension Plan Accrual = [1.0% x \$61,600 + 1.5% (\$140,000-\$61,600)] x 0.4167

= [\$616 + \$1,176] x 0.4167 = \$746.73

ITA Maximum Accrual = \$3,245.56 x 0.4167 = \$1,352.42

2021 PA = 9 x min (\$746.73, \$1,352.42) - 600 = \$6,121

Total 2021 PA = \$8,020+ \$6,121 = \$14,141

Member D

2021 PA formula = (9 x 2021 DB accrual) – 600 2021 service = 2/12 = 0.1667 2021 Pension Plan Accrual = [1.0% x 30,000] x 0.1667 = [300] x 0.1667 = 50 ITA Maximum Accrual = \$3,245.56 x 0.1667= 541.03 2021 PA = 9 x min (\$50, \$541.03) – 600 = -\$150 Since calculated PA is negative, **2021 PA = \$0**